
Study of Isospin Fluctuations at RHIC-PHENIX

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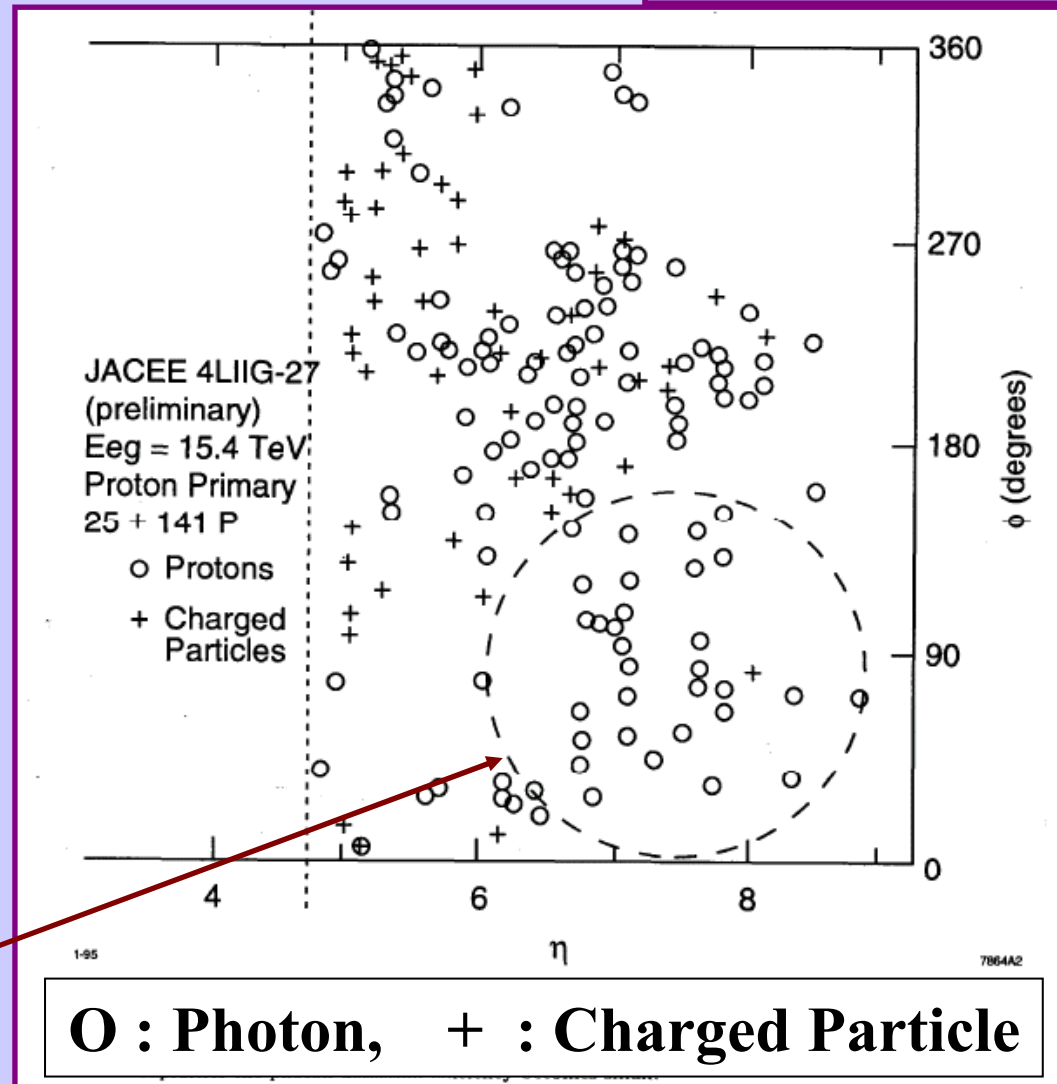
Centauro /Anti Centauro Event

Anti Centauro

(Cosmic ray experiment)

- (Brazil-Japan collaboration in Bolivia)
Y.Fujimoto and
S.Hasegawa, Phys. Rep. 65,
151 (1980)
- (JACEE) J.J.Lord and
Iwai, Paper No. 515,
International Conference
on High Energy Physics,
Dallas (1992)

This is anomalous
region assuming
isospin symmetry.



List of Centauro Searches

	Experiment	Collaboration	CM Energy	Search Region (η, ϕ)
1980	Mt. Chacaltaya	Brazil-Japan	$\sqrt{s} \geq 1.7 \text{ TeV}$	-----
1992	Balloon	JACEE	-----	$5.0 < \eta < 9.0$ $\Delta\phi < 2\pi$
1982	SPPS	UA5	$\sqrt{s} = 540 \text{ GeV}$	$ \eta < 5.0$
1983	SPPS	UA1	$\sqrt{s} = 540 \text{ GeV}$	$ \eta < 3.1$
1986	SPPS	UA5	$\sqrt{s} = 900 \text{ GeV}$	$ \eta < 5.0$
1996	TEVATRON	CDF	$\sqrt{s} = 1.8 \text{ TeV}$	$ \eta < 4.2, \Delta\phi < 2\pi$
1997	TEVATRON	MINIMAX	$\sqrt{s} = 1.8 \text{ TeV}$	$3.4 < \eta < 4.2$
2000	SPS	WA98	$\sqrt{s} = 3.5 \text{ TeV (Pb+Pb)}$	$2.80 < \eta < 3.75$ $\Delta\phi < \pi$
2001	RHIC	PHENIX	$\sqrt{s} = 39.4 \text{ TeV}$ (Run2 Au+Au)	$ \eta < 0.35$ $\Delta\phi < 1/2 \pi (\times 2 \text{ arm})$

PHENIX Experiment at Run2

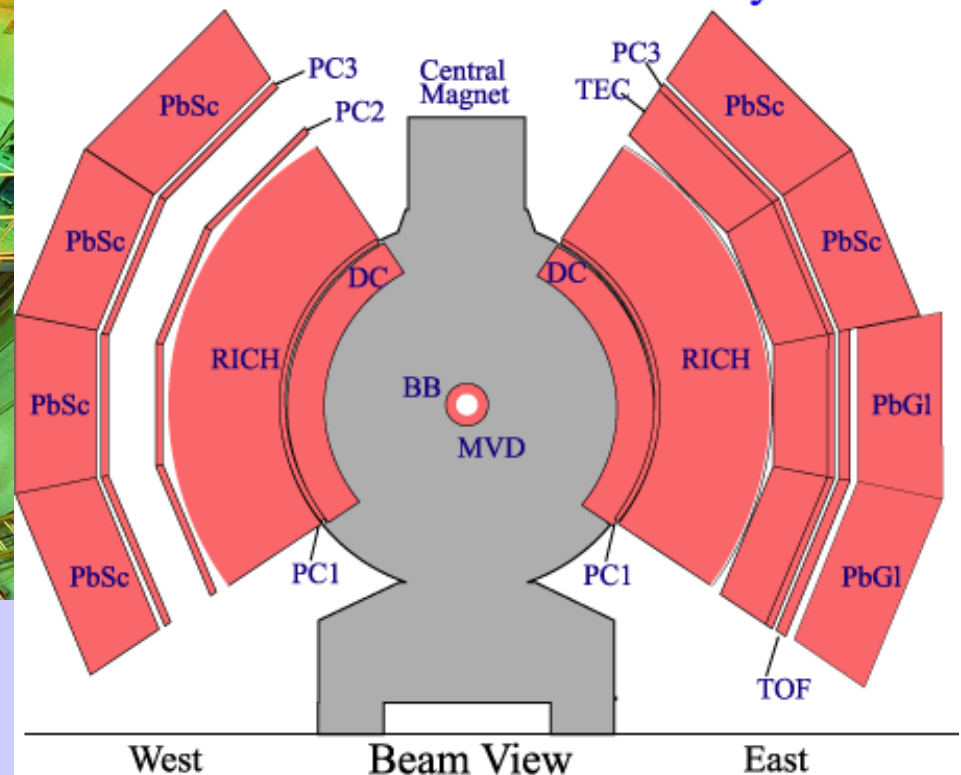
Using Magnetic Field-off data

Gamma-like Cluster (Electro-Magnetic Calorimeter)

Charged Track (Drift Chamber and Pad Chamber1)



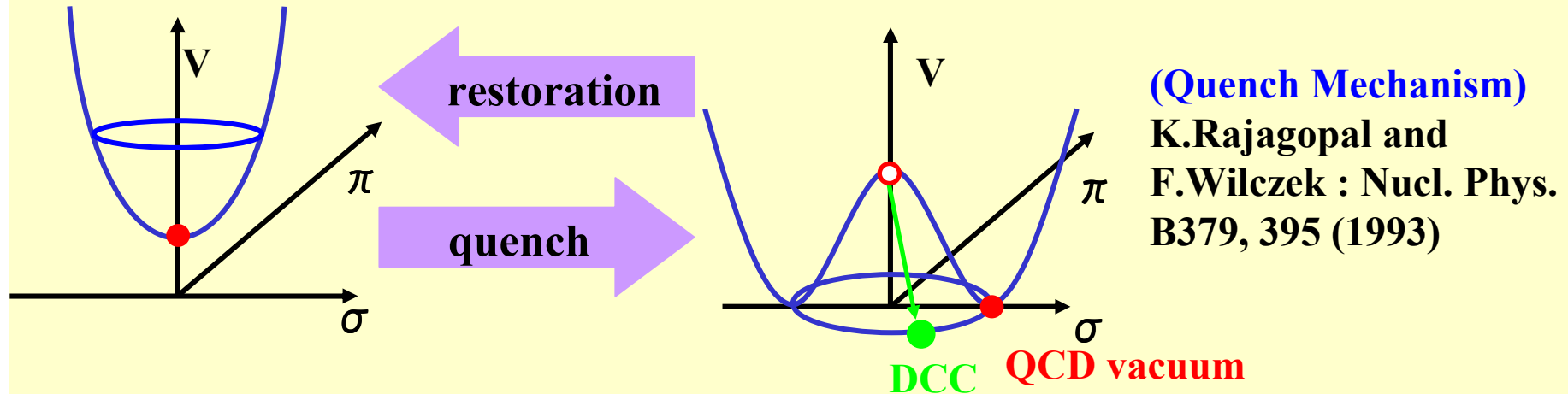
PHENIX Detector - Second Year Physics Run



$$-0.35 < \eta < 0.35$$

$$\Delta\phi < 1 / 2 \pi \text{ in each arm}$$

Disoriented Chiral Condensate



Chiral transformation

$$\begin{pmatrix} u \\ d \end{pmatrix} \rightarrow e^{i\gamma^5 \tau \cdot \theta} \begin{pmatrix} u \\ d \end{pmatrix}$$

Linear sigma model

$$\phi_i = (\sigma, \pi)$$

$$L = \frac{1}{2} \partial_\mu \phi_i \partial^\mu \phi_i - \frac{1}{4} (\phi^2 - v^2)^2 + \underline{H\sigma}$$

**Chiral symmetry breaking term
due to finite masses**

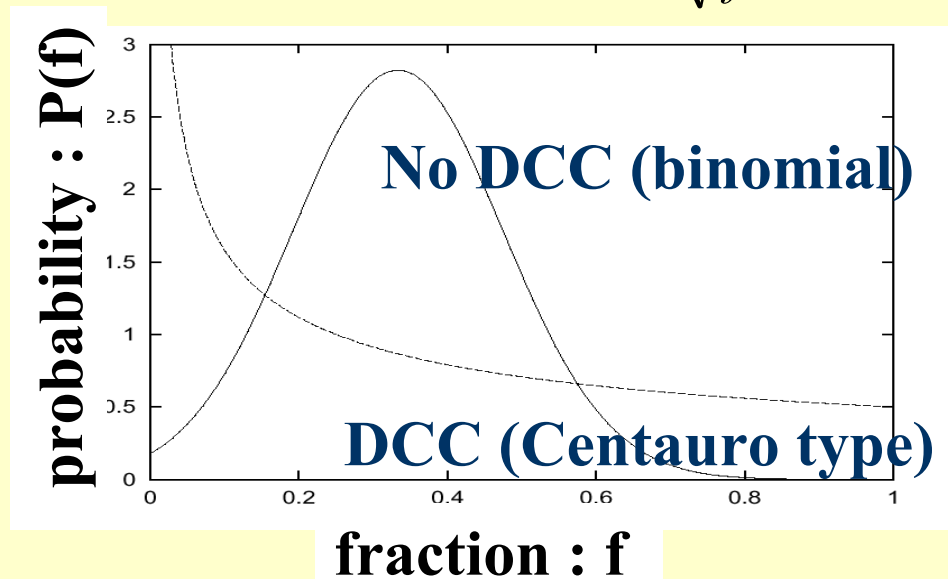
Search Strategy

If every event could contain largely deviated domains on isospin symmetry and most of domains per event could be detected within a limited detector acceptance, we would be able to discuss anomaly based on the probability distribution by the statistical treatment like:

However, we do not know domain information on the numbers and sizes a priori, and our detector acceptance is very limited. Therefore we need to search for rare events containing anomalous domain like cosmic ray experiments rather than statistical treatment above.

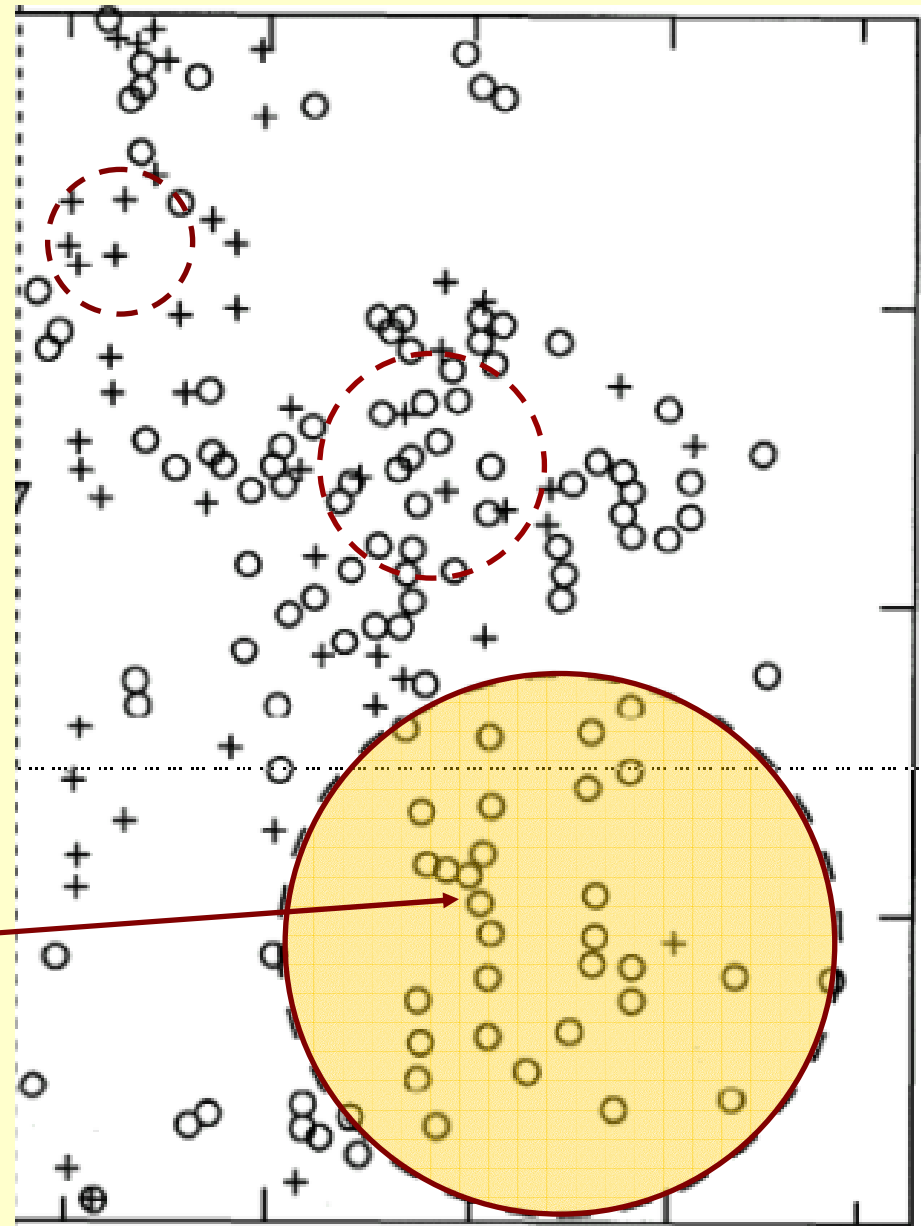
$$\text{fraction} : f = \frac{n_{\pi^0}}{n_{\pi^0} + n_{\pi^+} + n_{\pi^-}}$$

$$\text{probability} : P(f)df = \frac{1}{2\sqrt{f}} df$$



We search for a most largely deviated domain per event by looking at differences between number of charged and gamma-like clusters by changing regions of interest as we do by eyes, because we don't know what the size is and where the position is.

We want to extract this region. We must do this search in several million events.

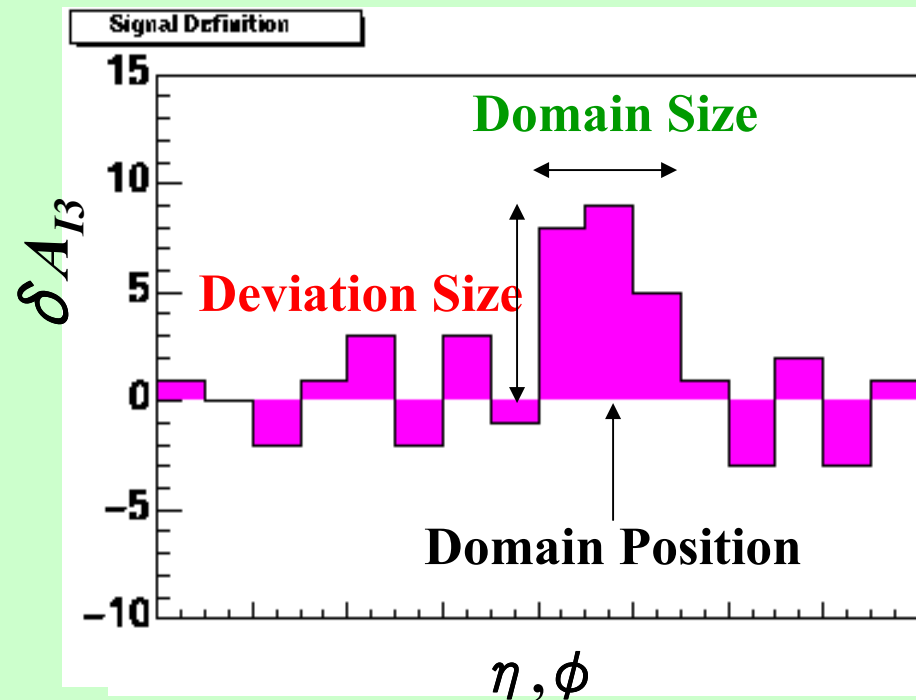


Observables

Definition of asymmetry between number of charged tracks and neutral clusters event-by-event base as a function of subdivided eta-phi phase spaces normalized by 1 sigma of standard deviation for given multiplicity.

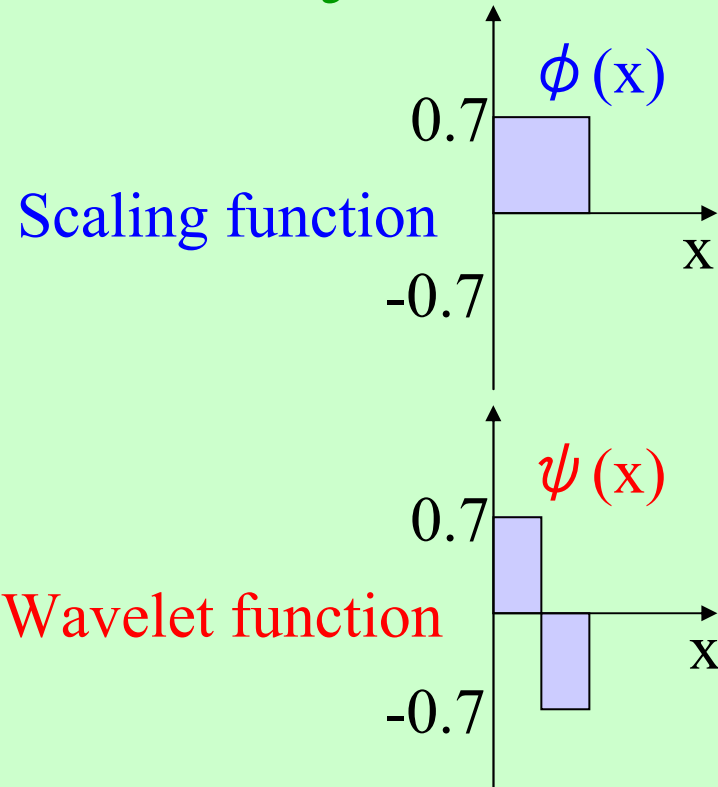
$$\delta A_{I_3}(\Delta\eta\Delta\phi) \equiv \frac{N_{\pi^\pm}(\Delta\eta\Delta\phi) - N_\gamma(\Delta\eta\Delta\phi)}{\sqrt{N_{\pi^\pm} + N_\gamma}}$$
$$\approx \frac{N_{ch}(\Delta\eta\Delta\phi) - N_\gamma(\Delta\eta\Delta\phi)}{\sqrt{N_{ch} + N_\gamma}}$$

Domain Size and Domain Position of large deviated region can be obtained at the same time by using Multi Resolution Analysis (MRA) technique.

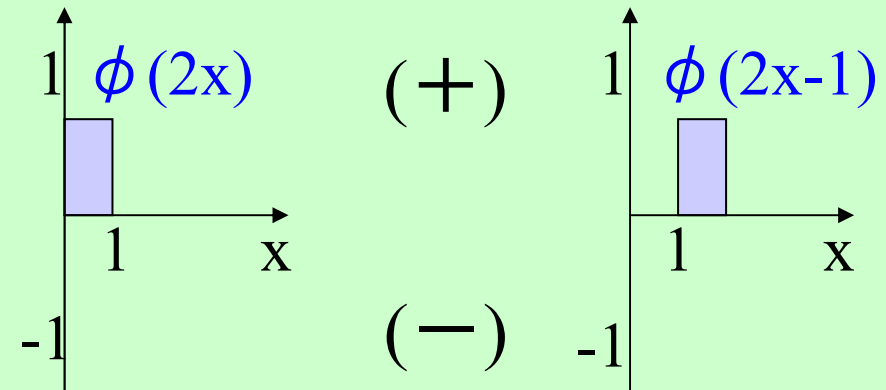


Multi Resolution Analysis (MRA)

Level $j-1$: 2^{j-1} bins



Level j : 2^j bins



$$\begin{aligned}\phi(2x) &= 1/\sqrt{2} \{ \phi(x) + \psi(x) \} \\ \phi(2x-1) &= 1/\sqrt{2} \{ \phi(x) - \psi(x) \}\end{aligned}$$

Total number of bins is 2^j

Level j correspond to resolution level

Decomposition

k : k-th bin in pseudo rapidity

C_{jk} : coefficients of ϕ

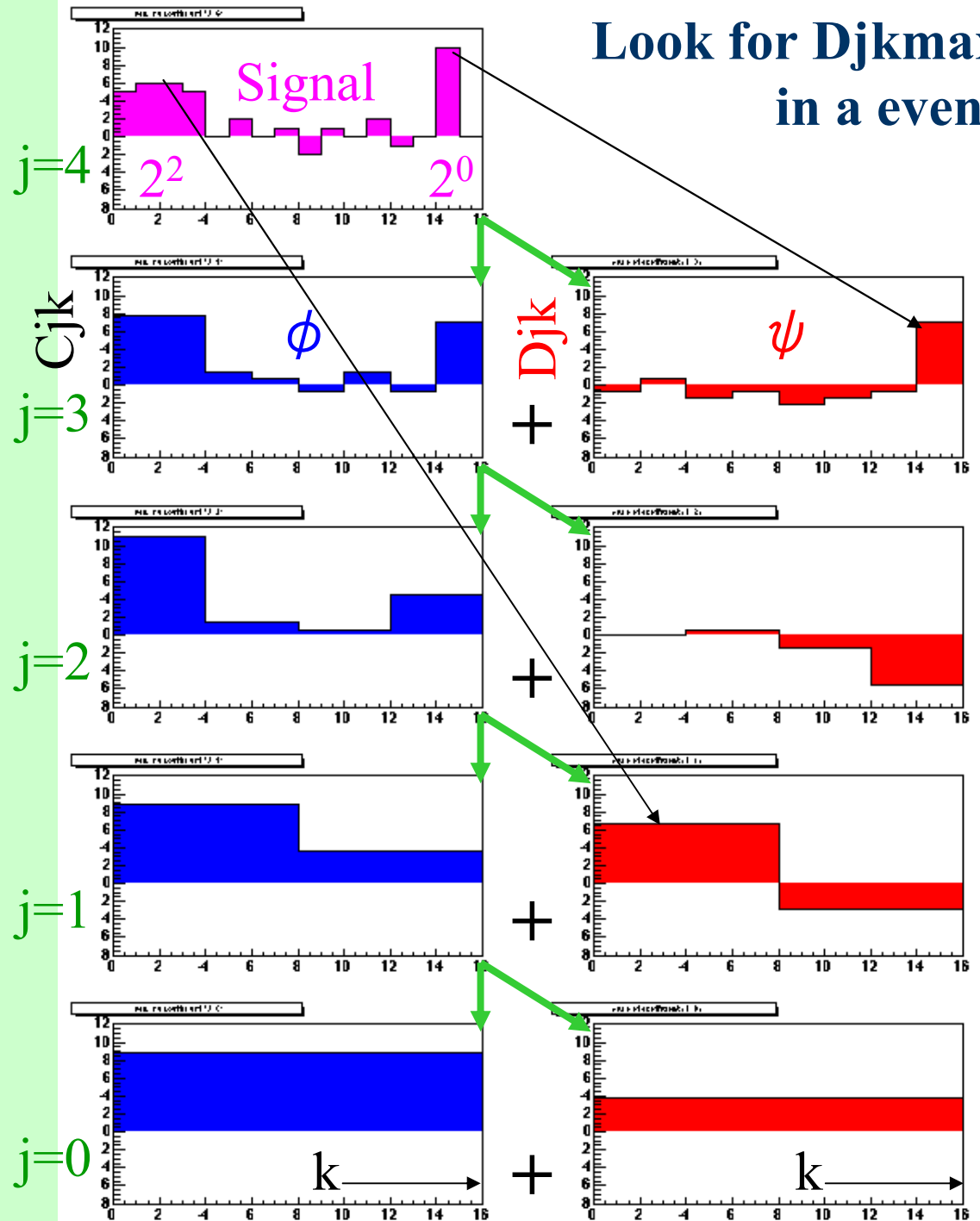
Djk : coefficients of ψ



1/2^j → Domain Size

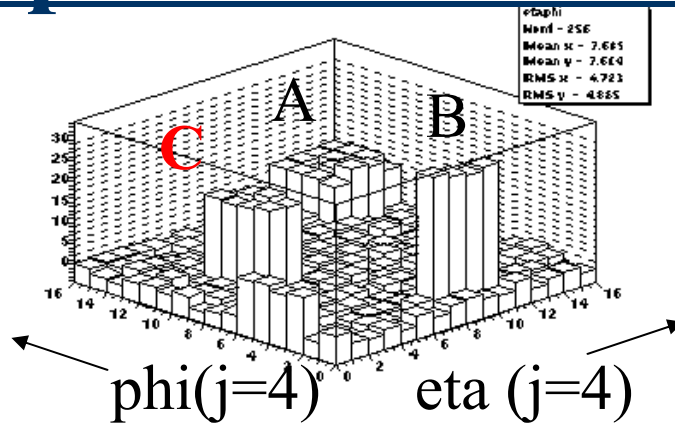
$\mathbf{k} \rightarrow$ Phase Space Position

Djk \rightarrow Deviation Size



Look for Djkmax in a event

Example of 2D MRA



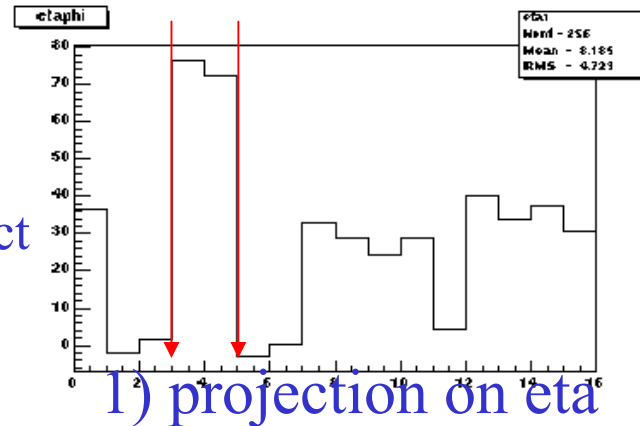
Domain C:
 $A_{I3} = \sim 20 \times 8 \text{ bins}$
 $(\eta, \phi) = (3, 7)$
 $(j_\eta, j_\phi) = (3, 2)$

Result: Correct

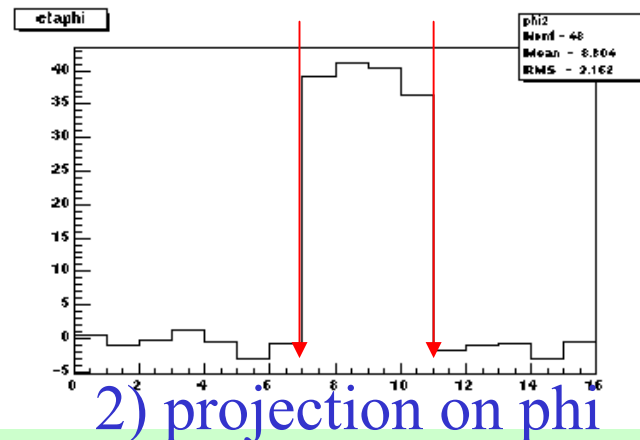
$(\eta, \phi) = (3, 7)$

$(j_\eta, j_\phi) = (3, 2)$

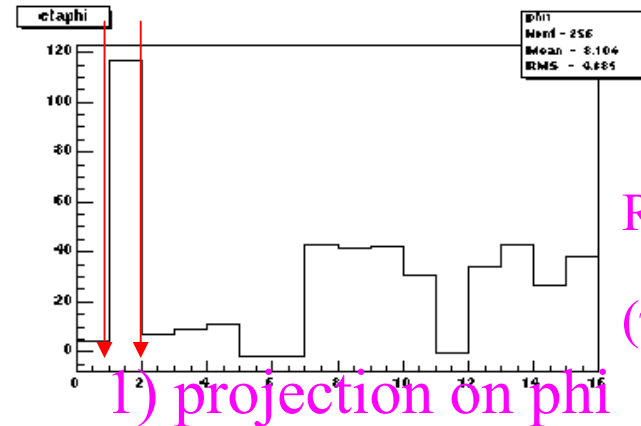
D_{jkmax}^2
 $= 4392.42$



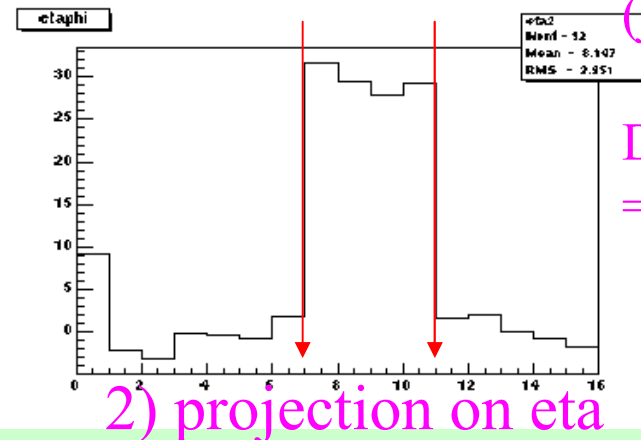
1) projection on eta



2) projection on phi



1) projection on phi



2) projection on eta

Result: Wrong

$(\eta, \phi) = (7, 1)$

$(j_\eta, j_\phi) = (2, 4)$

D_{jkmax}^2
 $= 3179.54$

Binomial Distribution as a Baseline Fluctuation

- We need to define a degree of the anomaly quantitatively with a familiar statistical language.
- Suppose that we have m charged tracks and n γ -clusters in our total detector acceptance in a given event. If we distribute them independently into the acceptance, the asymmetry found in a given subdivided phase space must follow asymmetry based on binomial distributions.
- We apply 2-D MRA to those simple binomial samples.
- We can get correspondence between Djkmax^2 and probability to exclude the binomial sample.

$$p^{(j_\eta, j_\phi)} \equiv 2^{-(j_\eta + j_\phi)}$$

$$B_m^{(j_\eta, j_\phi)}(x) \equiv {}_m C_x \{p^{(j_\eta, j_\phi)}\}^x \{1 - p^{(j_\eta, j_\phi)}\}^{m-x}$$

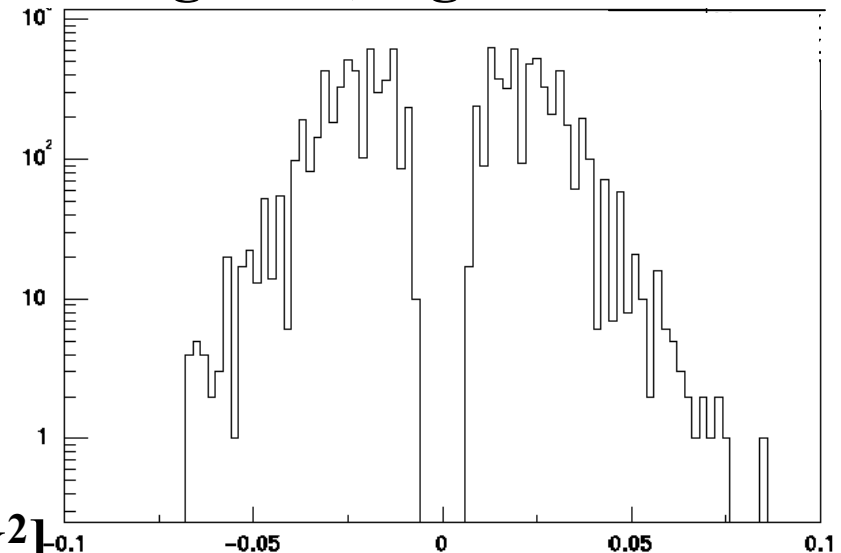
$$B_n^{(j_\eta, j_\phi)}(y) \equiv {}_n C_y \{p^{(j_\eta, j_\phi)}\}^y \{1 - p^{(j_\eta, j_\phi)}\}^{n-y}$$

$$d \equiv x - y = \delta A_{I3} \cdot \sqrt{m + n}$$

$$P_{(m,n)}^{(j_\eta, j_\phi)}(d) = \sum_{i=\max(d,0)}^{\min(n,m+d)} B_n^{(j_\eta, j_\phi)}(i) B_m^{(j_\eta, j_\phi)}(i-d)$$

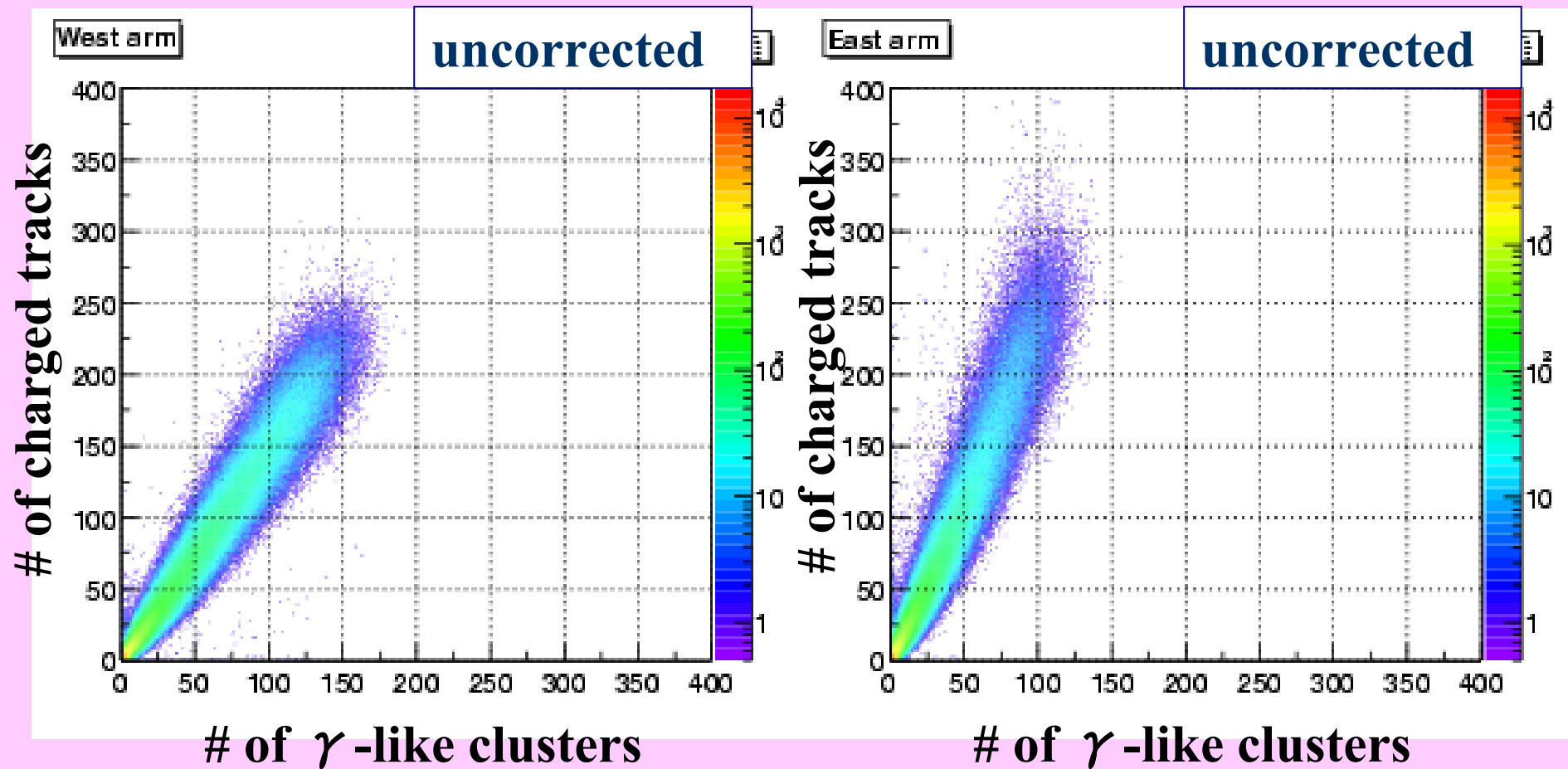
$$m \geq 0, n \geq 0, -m \leq d \leq n$$

#charge:100, #gamma-like:100



[Djkmax²]

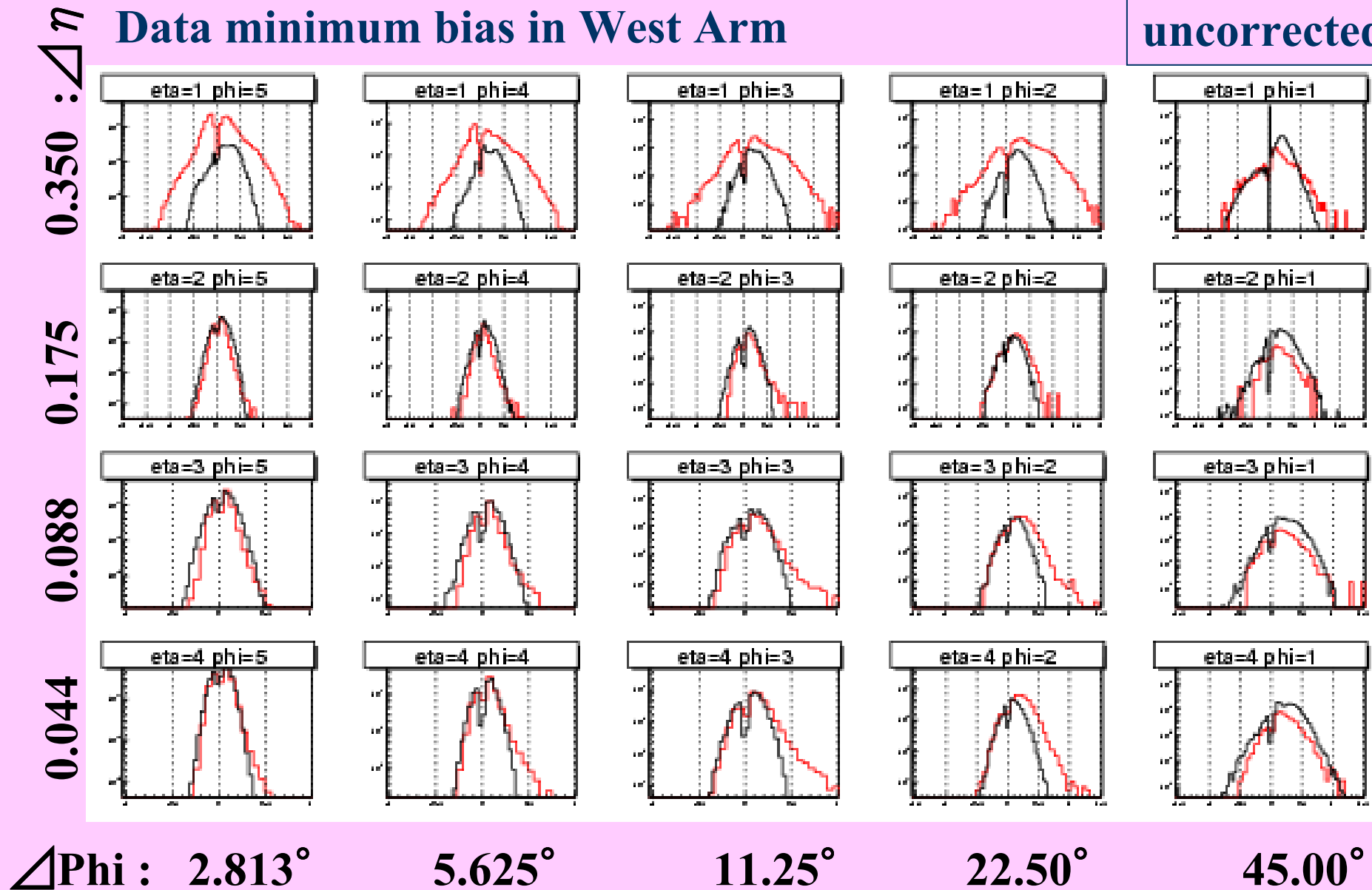
Correlation between Charged Tracks and Gamma-like Clusters



Maximum Deviation Size (D_{jkmax}^2)

Data minimum bias in West Arm

uncorrected

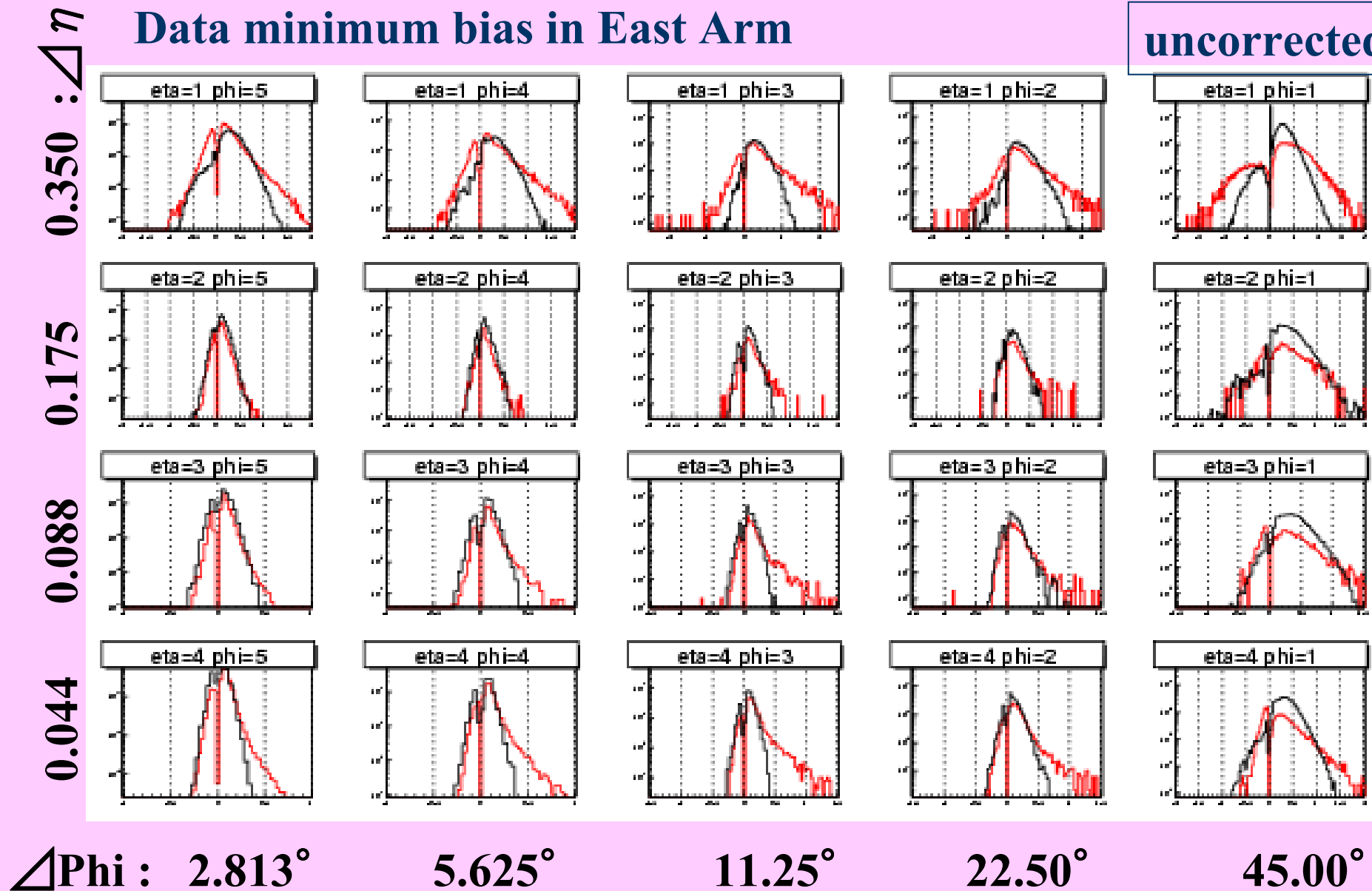


- Red : Data
- Black : Binomial

(# of charge > 1, # of gamma > 1)

Data minimum bias in East Arm

uncorrected



Maximum Deviation Size (D_{jkmax}^2)

HIJING minimum bias in West Arm

uncorrected

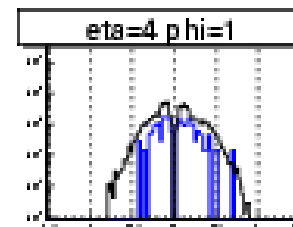
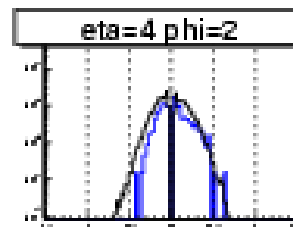
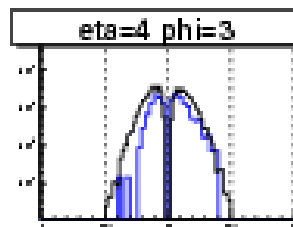
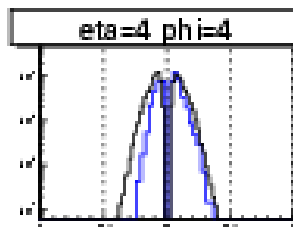
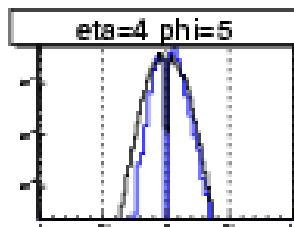
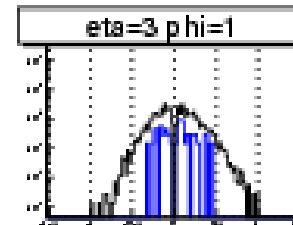
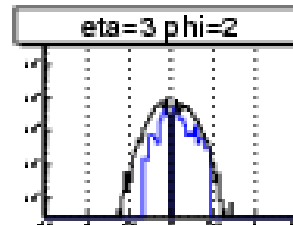
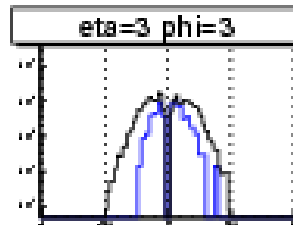
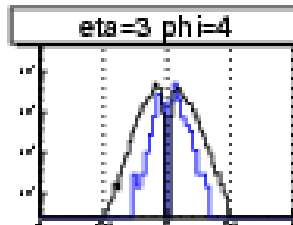
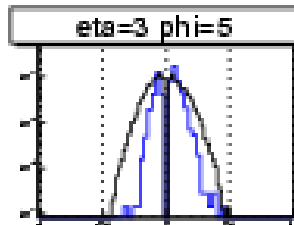
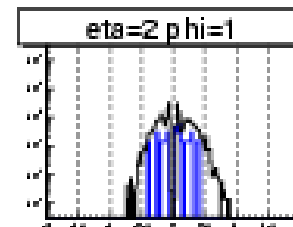
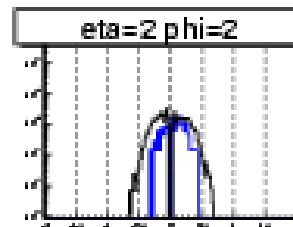
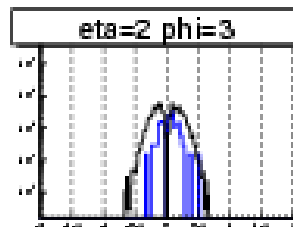
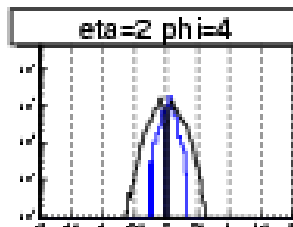
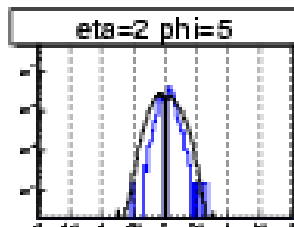
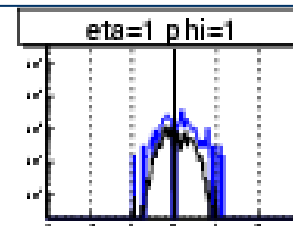
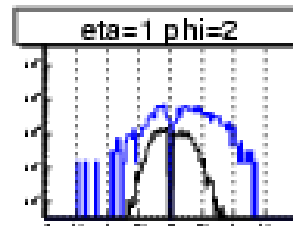
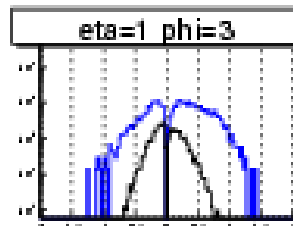
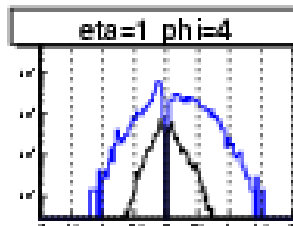
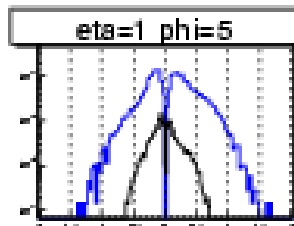
$\Delta\eta$

0.350

0.175

0.088

0.044



$\Delta\Phi$: 2.813°

5.625°

11.25°

22.50°

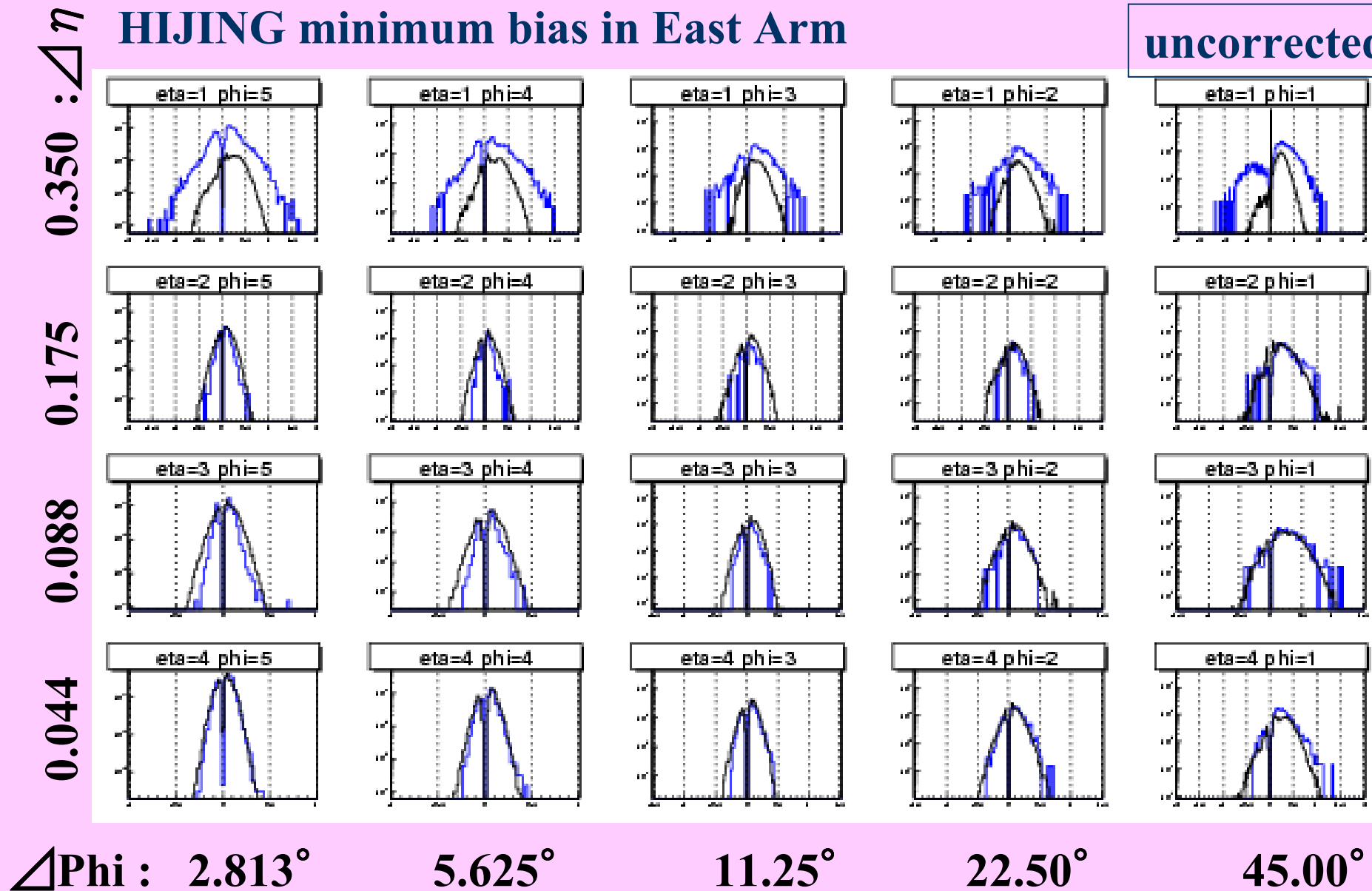
45.00°

- Blue : HIJING
- Black : Binomial

(# of charge > 1, # of gamma > 1)

HIJING minimum bias in East Arm

uncorrected



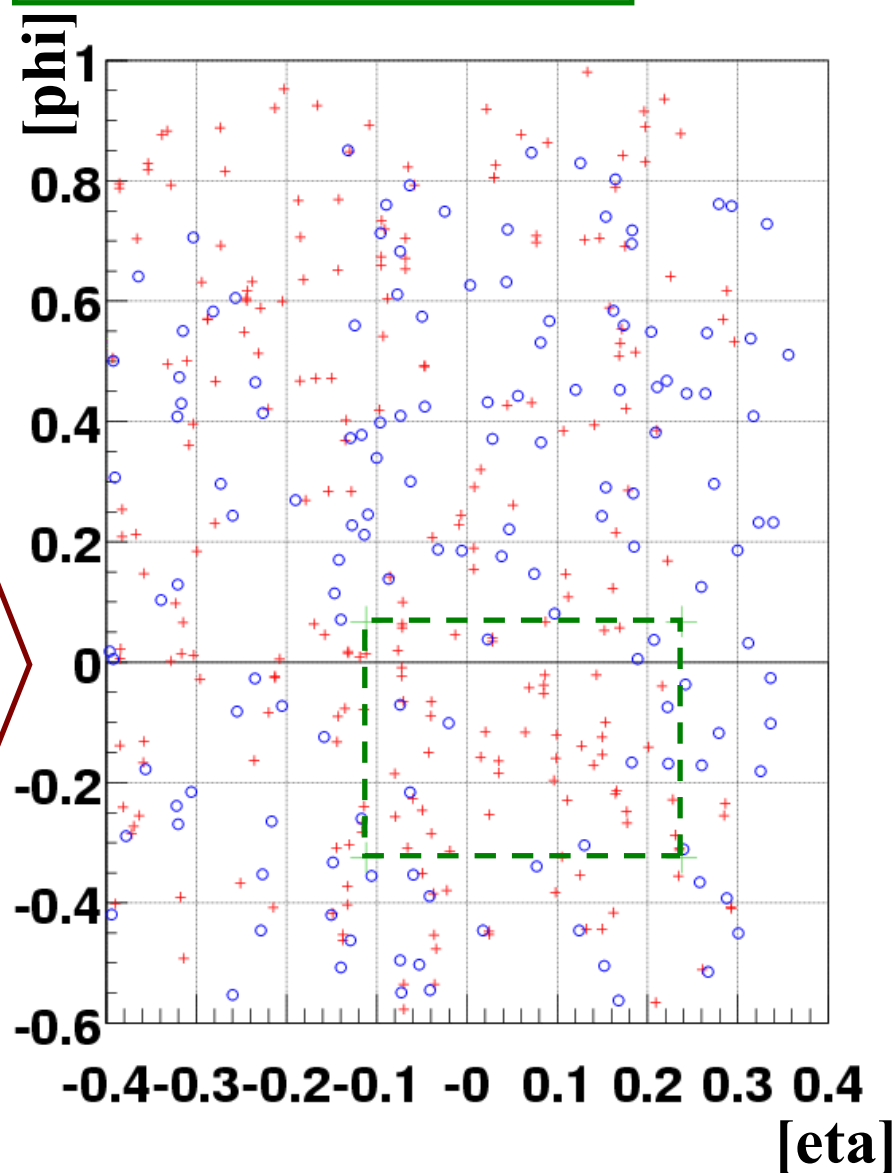
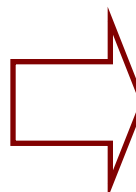
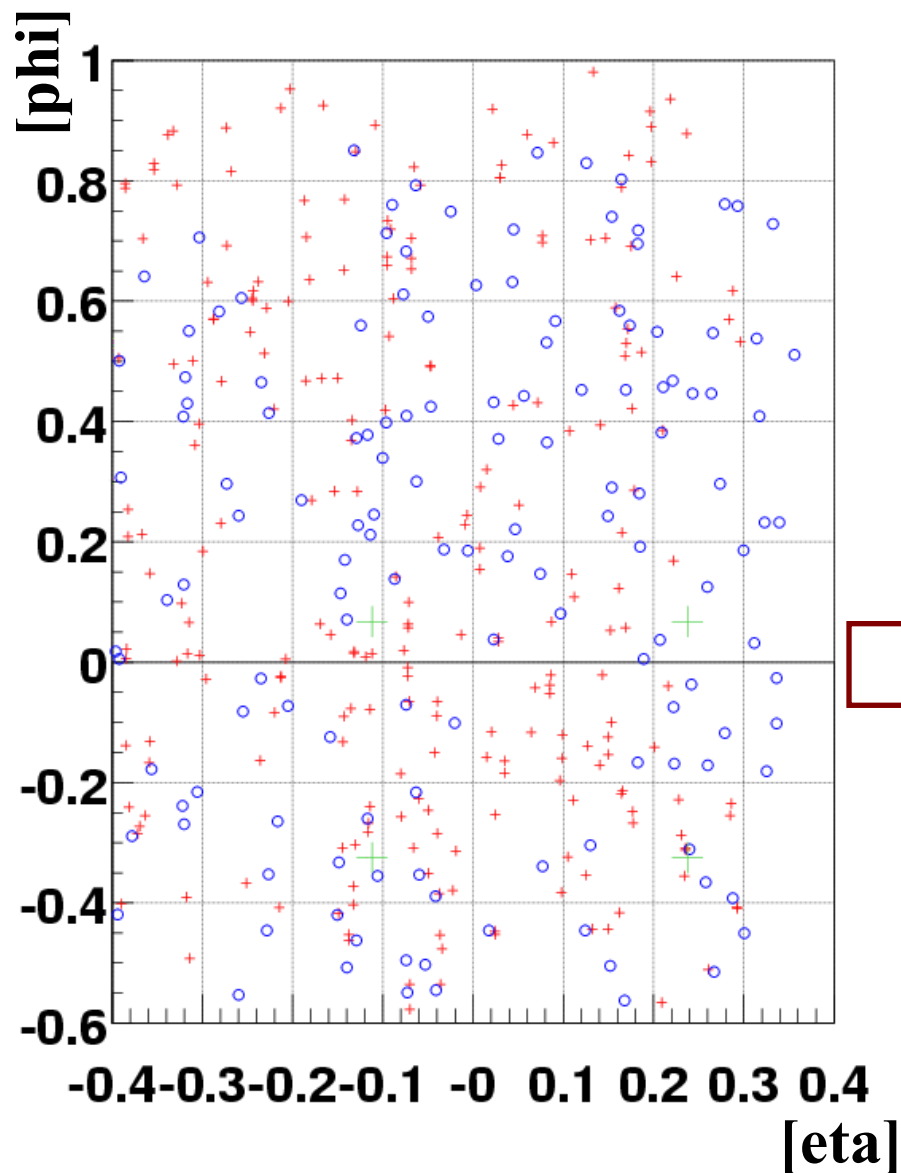
Centauro Type (West)

Djkmax² : 1.698

of gamma-like : 10

of charged : 55

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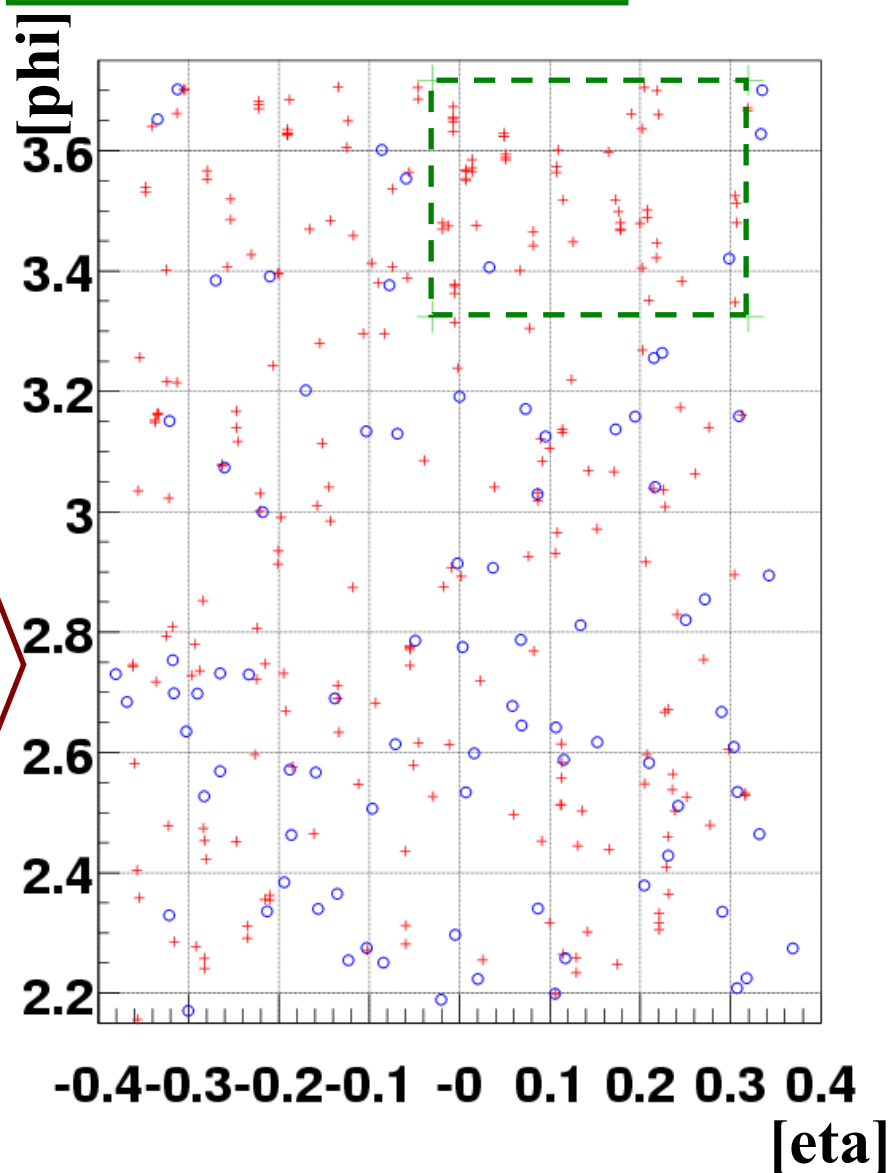
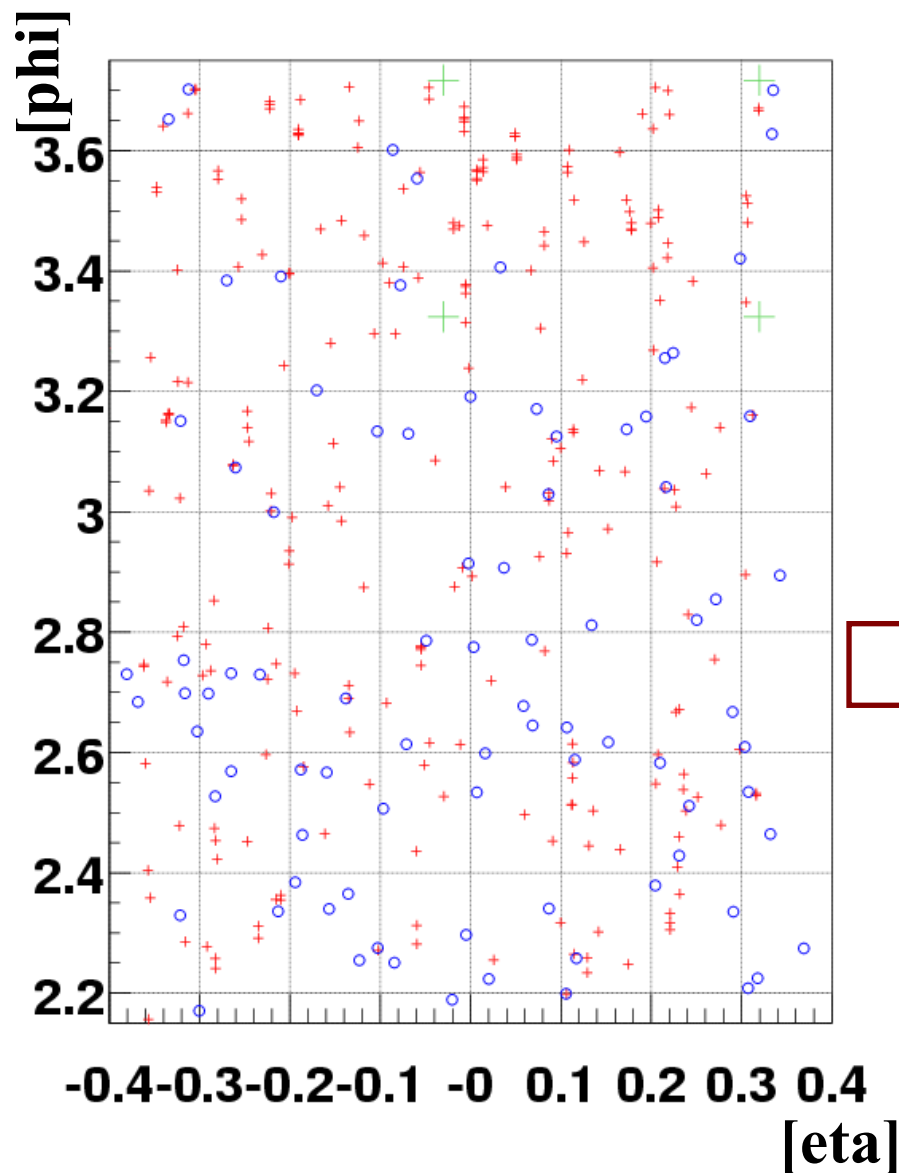
Centauro Type (East)

Djkmax² : 2.251

of gamma-like : 2

of charged : 49

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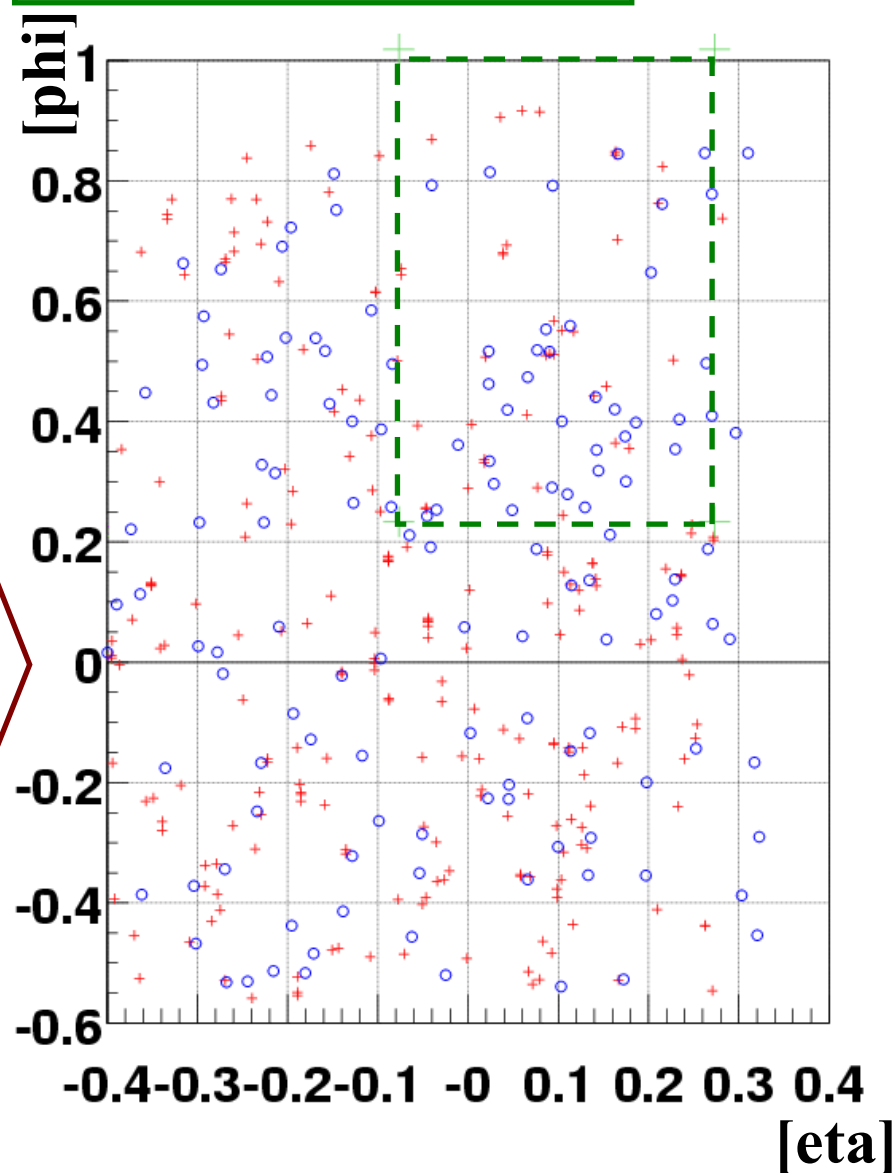
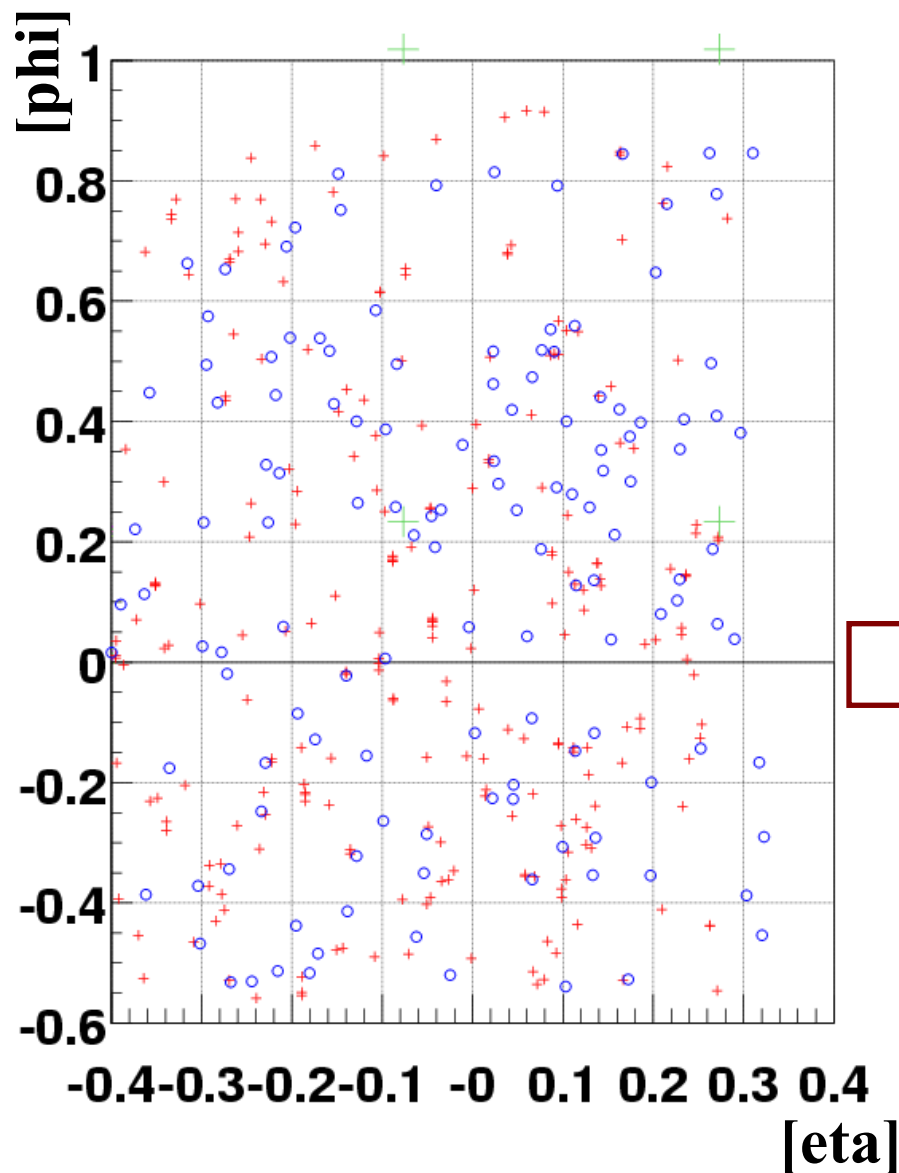
Anti Centauro Type

$D_{j\text{max}}^2 : -1.638$

of gamma-like : 36

of charged : 28

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Summary and Future Plan



- **We have demonstrated two dimensional multi-resolution analysis on the asymmetry between the number of the charged tracks and γ -like clusters in the $\eta - \phi$ phase space. (See below)**
- **More understanding of detector biases is necessary.**
- **Set a reasonable significance level to define the degree of anomaly based on the physical models with normal fluctuations.**
- **Count the anomalous events above the significance level.**
- **Discuss the event characters of those events, if they are found.**